## Post graduate Exam (Basic Engineering Sciences)

 Branch: Engineering Mathematics (Master 600)Menofia University
Faculty of Engineering Shebin El-Kom
Academic Year: 2017-2018
Department: Basic Eng. Sci.

Subject: Ordinary Differential Equations (1)
Code : BES 609
Time Allowed: 3 hours
Date: $30 / 5 / 2018$
Total Marks: 100 Marks

Answer all the following questions:
Q. 1 (A) Find the general solution of the following differential equation :-

$$
\frac{x d x+y d y}{x d y-y d x}=\sqrt{\frac{a^{2}-x^{2}-y^{2}}{x^{2}+y^{2}}}
$$

(B) Solve the following differential equation by homogeneous method:-

$$
z\left(x^{2}-y z-z^{2}\right) d x+x z(x+z) d y+x\left(z^{2}-x y-x^{2}\right) d z=0
$$

(C) Solve the following differential equation by parametric method:-

$$
x d x+y d y+\left(x^{2}+y^{2}+z^{2}+1\right) z d z=0
$$

Q. 2 (A) Solve the following simultaneous differential equations:-

1) $\frac{d x}{y z}=\frac{d y}{x z}=\frac{d z}{x y}$
2) $\frac{x d x}{y^{3} z}=\frac{d y}{x^{2} z}=\frac{d z}{y^{3}}$
(B) Solve the following simultaneous total differential equations:-
$y z d x+x z d y+x y d z=0$ and $(x z+x y-y z) d x+x^{2} d y+x^{2} d z=0$
(C) Solve the following differential equations:-
3) $y^{\prime \prime \prime}+y^{\prime \prime}=x$
4) $\left(y^{\prime \prime}\right)^{2}-2 x y^{\prime \prime} y^{\prime \prime \prime}+\left(y^{\prime \prime \prime}\right)^{2}\left(x^{2}-1\right)=1$
Q. 3 (A) Solve the following differential equations by method of variation of parameters:-
5) $y^{\prime \prime}+y=x^{2} e^{x}$
6) $y^{\prime \prime}-2 y^{\prime}+y=\frac{1}{x} e^{x}$
7) $y^{\prime \prime \prime}+y^{\prime}=\tan x$
(B) Solve the following initial value problem by Laplace transform method :$y^{\prime \prime}-2 y^{\prime}+5 y=8 \sin t-4 \cos t$ with intial conditions at $t=0$, $y(0)=1$, and $y^{\prime}(0)=3$
(C) Find the total solution of the following system of differential equations by Laplace transform method :-
$\frac{d^{2} y}{d t^{2}}-y=3 x$ and $\frac{d^{2} x}{d t^{2}}-4 y=-4 e^{t}$
with intial conditions at $t=0$,
$y(0)=2, y^{\prime}(0)=3, x(0)=1$, and $x^{\prime}(0)=2$
[Q. 3 (25 mark)]
Q. 4 (A) Solve the following differential equations in power series using Frobenius method:-
$\left(1-x^{2}\right) y^{\prime \prime}-2 x y^{\prime}+2 y=0$
(B) Solve the following differential equations in power series using

Frobenius method when $x$ has very large value:-
$2 x^{3} y^{\prime \prime}+x^{2} y^{\prime}+y=0$
(C) Find the general solution of the following system of differential equations:

$$
\begin{aligned}
& D x+D y \quad=2 \sinh t \\
& D v+D z=e^{t} \\
& D x \quad+D z=2 e^{t}+e^{-t} \\
& \text { where } D=\frac{d}{d t}
\end{aligned}
$$

[Q. 3 (25 mark)]
Wíth my best wishes

